

A Proper Security Level for Postcompromise Secure Messaging

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EPFL



New logo!

LASEC

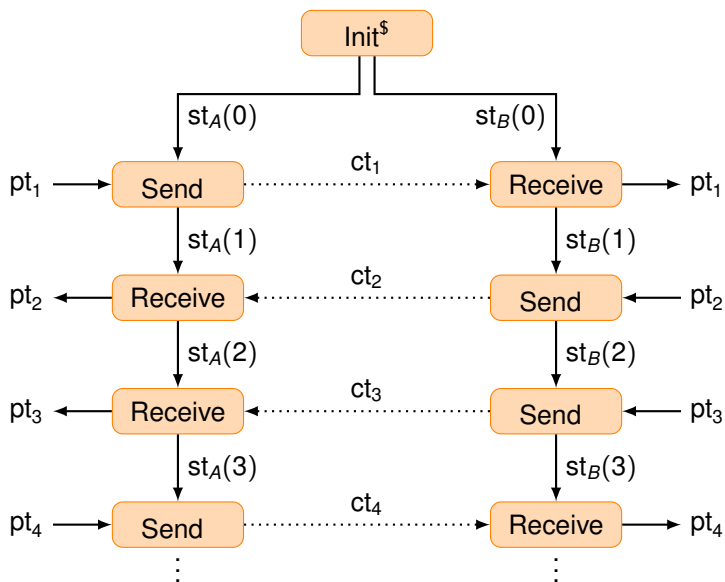
- 1 Ratcheting
- 2 BARK
- 3 ARCAD
- 4 Comparison of Protocols

- 1 Ratcheting**
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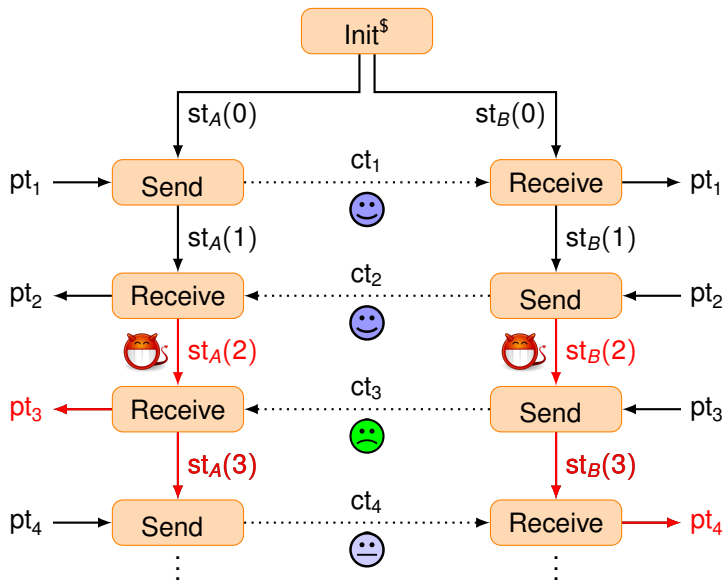
End-To-End Secure IM



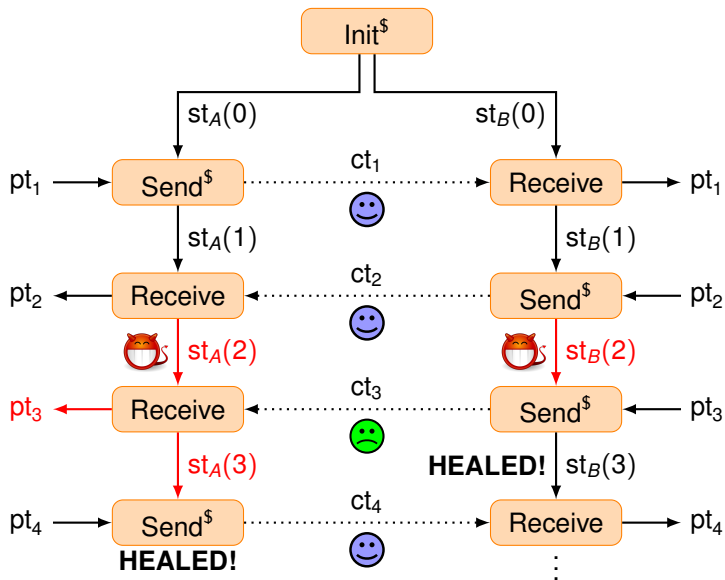
Secure Bidirectional Communication



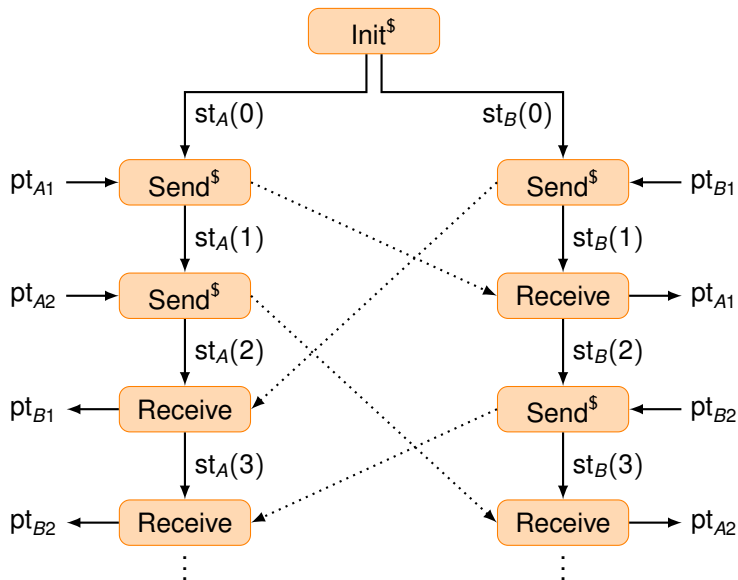
Aim: Forward Secrecy



Aim: + Post-Compromise Security

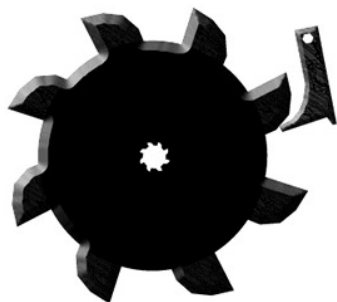


By the Way: Asynchronous + Random Role





Ratchet



state update

- in a one-way manner (for **forward security**)
- using randomness (for **post-compromise security**)

Bellare, Singh, Asha, Jaeger, Nyayapati, Stepanovs
Ratcheted Encryption and Key Exchange: The Security of Messaging

- unidirectional
- no receiver leakage allowed
- complicated definitions

Poettering, Rösler

Ratcheted Key Exchange, Revisited

Jaeger, Stepanovs

Optimal Channel Security Against Fine-Grained State Compromise: The Safety of Messaging

- both need key update primitives (HIBE, random oracles, ...)
- complicated definitions

with immediate decryption

Alwen, Coretti, Dodis

The Double Ratchet: Security Notions, Proofs, and Modularization for the Signal Protocol

Jost, Maurer, Mularczyk

Efficient Ratcheting: Almost-Optimal Guarantees for Secure Messaging

near-optimal security but better complexity — still high

Our Results

Durak, Vaudenay

*Bidirectional Asynchronous Ratcheted Key Agreement
with Linear Complexity*

Eprint 2018/889

Caforio, Durak, Vaudenay

On-Demand Ratcheting with Security Awareness

Soon on Eprint

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- 2 BARK**
- 3 ARCAD
- 4 Comparison of Protocols

BARK

Bidirectional Asynchronous Ratcheted Key Agreement



Interface

- $\text{Setup}(1^\lambda) \xrightarrow{\$} \text{pp}$ (the common public parameters)
- $\text{Gen}(\text{pp}) \xrightarrow{\$} (\text{sk}, \text{pk})$ (key pair of a participant)
- $\text{Init}(\text{pp}, \text{sk}_P, \text{pk}_{\bar{P}}, P) \rightarrow \text{st}_P$ (initial state)
- $\text{Send}(\text{st}_P) \xrightarrow{\$} (\text{st}'_P, \text{ct}, k)$ (like KEM.Enc)
- $\text{Receive}(\text{st}_P, \text{ct}) \rightarrow (\text{acc}, \text{st}'_P, k)$ (like KEM.Dec)

Initall(pp):

- 1: $\text{Gen}(\text{pp}) \rightarrow (\text{sk}_A, \text{pk}_A)$
- 2: $\text{Gen}(\text{pp}) \rightarrow (\text{sk}_B, \text{pk}_B)$
- 3: $\text{st}_A \leftarrow \text{Init}(\text{pp}, \text{sk}_A, \text{pk}_B, 0)$
- 4: $\text{st}_B \leftarrow \text{Init}(\text{pp}, \text{sk}_B, \text{pk}_A, 1)$
- 5: $Z \leftarrow (\text{pp}, \text{pk}_A, \text{pk}_B)$
- 6: **return** $(\text{st}_A, \text{st}_B, Z)$

we must specify what to give to the adversary



Correctness

of form (P, send) or (P, rec)

For all sequence **sched**, $\Pr[\text{Correctness}(\text{sched}) \rightarrow 1] = 0$

Oracle RATCH(P, send)

- 1: $(st_P, ct_P, k_P) \leftarrow \text{Send}(st_P)$
- 2: append k_P to $\text{sent}_{\text{key}}^P$
- 3: **return** ct_P

Oracle RATCH(P, rec, ct)

- 4: $(acc, st'_P, k'_P) \leftarrow \text{Receive}(st_P, ct)$
- 5: **if** acc **then**
- 6: $st_P \leftarrow st'_P$
- 7: $k_P \leftarrow k'_P$
- 8: append k_P to $\text{received}_{\text{key}}^P$
- 9: **end if**
- 10: **return** acc

Game Correctness(**sched**)

- 1: Setup $\xrightarrow{\$}$ pp
- 2: $\text{Inital}(pp) \xrightarrow{\$}$ (st_A, st_B, z)
- 3: initialize two FIFO $\text{incoming}_P, P \in \{A, B\}$
- 4: $i \leftarrow 0$
- 5: **loop**
- 6: $i \leftarrow i + 1$
- 7: $(P, \text{role}) \leftarrow \text{sched}$;
- 8: **if** $\text{role} = \text{send}$ **then**
- 9: $ct \leftarrow \text{RATCH}(P, \text{send})$
- 10: push ct to $\text{incoming}_{\bar{P}}$
- 11: **else**
- 12: **if** incoming_P is empty **then return 0**
- 13: pull ct from incoming_P
- 14: $acc \leftarrow \text{RATCH}(P, \text{rec}, ct)$
- 15: **if** $acc = \text{false}$ **then return 1**
- 16: **end if**
- 17: **if** $\text{received}_{\text{key}}^A$ not prefix of $\text{sent}_{\text{key}}^B$ **then return 1**
- 18: **if** $\text{received}_{\text{key}}^B$ not prefix of $\text{sent}_{\text{key}}^A$ **then return 1**
- 19: **end loop**

KIND Security

For all ppt \mathcal{A} , $\left| \Pr \left[\text{KIND}_{0, C_{\text{clean}}}^{\mathcal{A}} \rightarrow 1 \right] - \Pr \left[\text{KIND}_{1, C_{\text{clean}}}^{\mathcal{A}} \rightarrow 1 \right] \right| = \text{negl}$

Game $\text{KIND}_{b, C_{\text{clean}}}^{\mathcal{A}}$

- 1: Setup $\xrightarrow{\$}$ pp
- 2: Initall(pp) $\xrightarrow{\$}$ (st_A, st_B, z)
- 3: $b' \leftarrow \mathcal{A}^{\text{RATCH}, \text{EXP}_{st}, \text{EXP}_{key}, \text{TEST}}(z)$
- 4: **if** $\neg C_{\text{clean}}$ **then return** \perp
- 5: **return** b'

exclude trivial attacks

- the EXP oracles can be used for trivial attacks without forgeries
- not easy to identify trivial attacks in the case of forgeries

Oracle $\text{TEST}(P)$

- 1: **if** $b = 1$ **then**
- 2: **return** k_P
- 3: **else**
- 4: **return** random $\{0, 1\}^{|k_P|}$
- 5: **end if**

Oracle $\text{EXP}_{key}(P)$

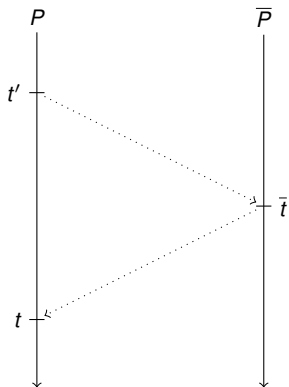
- 1: **return** k_P

Oracle $\text{EXP}_{st}(P)$

- 1: **return** st_P

A Few Technical Notions: Matching Status

$$P \text{ in matching status at time } t \iff \exists \bar{t}, t' \begin{cases} t' \leq t \\ \text{received}_{\text{msg}}^P(t) = \text{sent}_{\text{msg}}^{\bar{P}}(\bar{t}) \\ \text{received}_{\text{msg}}^{\bar{P}}(\bar{t}) = \text{sent}_{\text{msg}}^P(t') \end{cases}$$



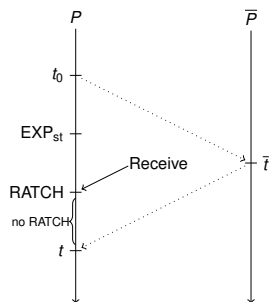
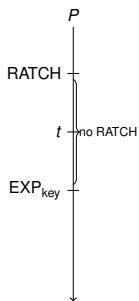
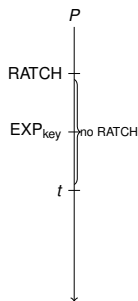
Property

If P in matching status at time t ...

- ... \bar{P} in matching status at time \bar{t}
- ... P in matching status before
- ... $k_P(t) = k_{\bar{P}}(\bar{t})$

A Few Technical Notions: Direct Leakage

$k_P(t)$ **directly leaks** if we are in one of those configurations:

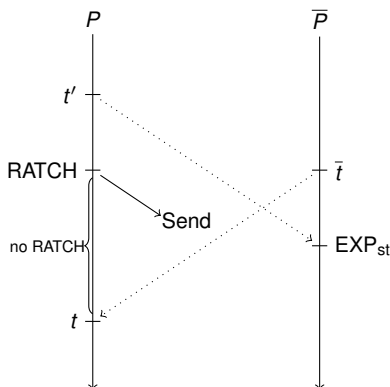


(P in matching status at time t)

A Few Technical Notions: Indirect Leakage

$k_P(t)$ **indirectly leaks** if P is in matching status at time t and

- either the corresponding $k_{\bar{P}}(\bar{t})$ directly leaks
- or we are in this configuration:



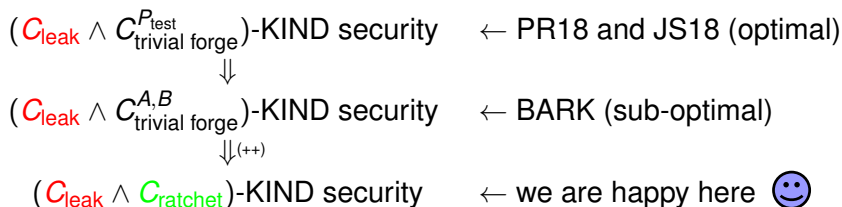
A Few Cleanness Notions

- C_{leak} : the tested $k_{P_{\text{test}}}$ leaks neither directly nor indirectly
mandatory: we must have this clause in C_{clean}
- $C_{\text{trivial forge}}^{P_{\text{test}}}$: P_{test} had no trivial forgery before TEST
- $C_{\text{trivial forge}}^{A,B}$: neither A nor B had a trivial forgery before seeing the ct making the tested $k_{P_{\text{test}}}$

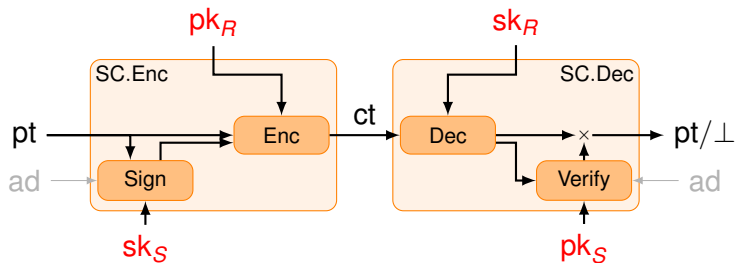
$$\begin{aligned} (C_{\text{leak}} \wedge C_{\text{trivial forge}}^{P_{\text{test}}})\text{-KIND security} &\leftarrow \text{PR18 and JS18 (optimal)} \\ \Downarrow & \\ (C_{\text{leak}} \wedge C_{\text{trivial forge}}^{A,B})\text{-KIND security} &\leftarrow \text{BARK (sub-optimal)} \end{aligned}$$

Why Optimal Security?

- seems to somehow imply HIBE...
- how would P_{test} know he accepted no forgery?
- by making sure that he can still communicate with $\overline{P}_{\text{test}}$
- \implies happy with
 C_{ratchet} : the ct making the tested $k_{P_{\text{test}}}$ initiated a round trip
 $P \xrightarrow{\text{ct}} \overline{P} \xrightarrow{\text{ct}'} P$

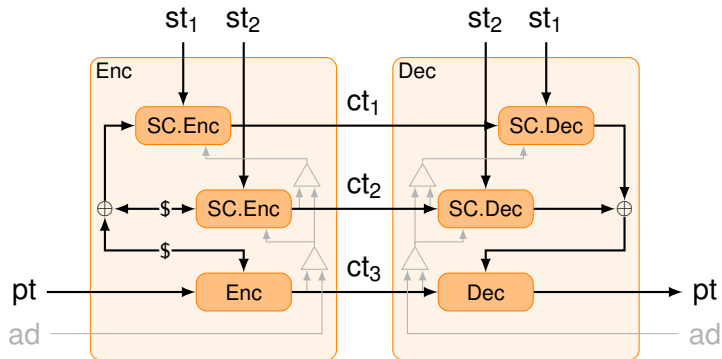


A Naive Signcryption

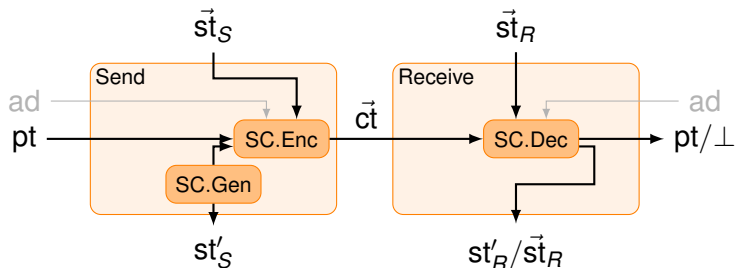


- encrypt and authenticate pt
- can authenticate ad at the same time
- sender state $st_S = (sk_S, pk_R)$
- receiver state $st_R = (sk_R, pk_S)$

Signcryption \rightarrow Multiple-Key Signcryption (Onion)

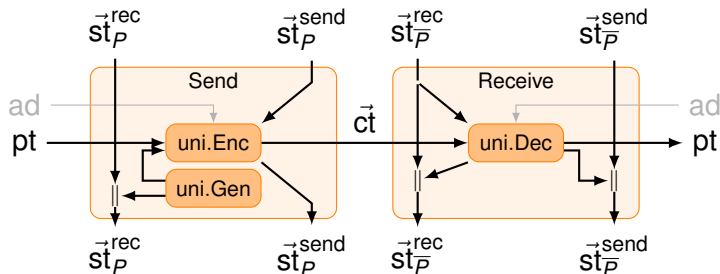


M-Key Signcryption \rightarrow Unidirectional Ratchet



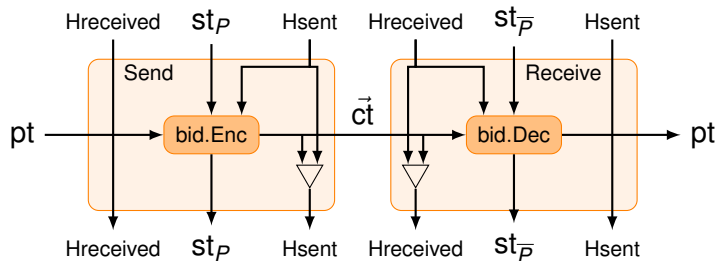
- generate the next send state while sending
- transmit the next receive state while sending
- flush all accumulated states

Unidirectional Ratchet → Bidirectional Ratchet



- generate a state for *replying* at sending
- accumulate receive states at sending

Bidirectional Ratchet \rightarrow BARK



- authenticate the chain of sent messages while sending

Our Protocol: BARK (Setup, Gen, Init)

BARK.Setup

- 1: $H.Gen(1^\lambda) \xrightarrow{\$} hk$
- 2: **return** hk

BARK.Gen(hk)

- 1: $SC.Gen_S \xrightarrow{\$} (sk_S, pk_S)$
- 2: $SC.Gen_R \xrightarrow{\$} (sk_R, pk_R)$
- 3: $sk \leftarrow (sk_S, sk_R)$
- 4: $pk \leftarrow (pk_S, pk_R)$
- 5: **return** (sk, pk)

BARK.Init($hk, sk_P, pk_{\bar{P}}, P$)

- 1: parse $sk_P = (sk_S, sk_R)$
- 2: parse $pk_{\bar{P}} = (pk_S, pk_R)$
- 3: $st_P^{send} \leftarrow (sk_S, pk_R)$
- 4: $st_P^{rec} \leftarrow (sk_R, pk_S)$
- 5: $st_P \leftarrow (hk, (st_A^{send}), (st_A^{rec}), \perp, \perp)$
- 6: **return** st_P

$$st = \left(\begin{array}{l} \langle \text{hash key} \rangle \\ \langle \text{list of send states} \rangle \\ \langle \text{list of receive states} \rangle \\ \langle \text{sent hash} \rangle \\ \langle \text{receive hash} \rangle \end{array} \right)$$

Our Protocol: BARK (Send)

BARK.Send(st_P)

- 1: parse $st_P = (hk, (st_P^{\text{send},1}, \dots, st_P^{\text{send},u}), (st_P^{\text{rec},1}, \dots, st_P^{\text{rec},v}), H\text{sent}, H\text{received})$
- 2: pick k
- 3: $\text{onion.Init}(1^\lambda) \xrightarrow{\$} (st_{\text{Snew}}, st_P^{\text{rec},v+1})$ ▷ append a new receive state to the st_P^{rec} list
- 4: $pt \leftarrow (st_{\text{Snew}}, k)$ ▷ then, st_{Snew} is erased to avoid leaking
- 5: take the smallest i s.t. $st_P^{\text{send},i} \neq \perp$ ▷ $i = u - n$ if we had n Receive since the last Send
- 6: $\text{onion.Send}(hk, st_P^{\text{send},i}, \dots, st_P^{\text{send},u}, H\text{sent}, pt) \xrightarrow{\$} (st_P^{\text{send},u}, ct)$ ▷ update $st_P^{\text{send},u}$
- 7: $st_P^{\text{send},i}, \dots, st_P^{\text{send},u-1} \leftarrow \perp$ ▷ flush the send state list: only $st_P^{\text{send},u}$ remains
- 8: $ct \leftarrow (H\text{sent}, ct)$ ▷ the onion has $u - i + 1 = n + 1$ layers
- 9: $H\text{sent}' \leftarrow H.\text{Eval}(hk, ct)$
- 10: $st'_P \leftarrow (hk, (st_P^{\text{send},1}, \dots, st_P^{\text{send},u}), (st_P^{\text{rec},1}, \dots, st_P^{\text{rec},v+1}), H\text{sent}', H\text{received})$
- 11: **return** (st'_P, ct)

- create a new onion channel for return
- add st^{rec} in list of receive states
- concatenate st_{Snew} to key
- onion.encrypt with all send states
- authenticate sent hash and the onion depth

Our Protocol: BARK (Receive)

BARK.Receive(st_P, ct)

- 1: parse $st_P = (hk, (st_P^{send,1}, \dots, st_P^{send,u}), (st_P^{rec,1}, \dots, st_P^{rec,v}), Hsent, Hreceived)$
- 2: parse $ct = (h, ct)$ ▷ the onion has $n + 1$ layers
- 3: set $n + 1$ to the number of components in ct
- 4: **if** $h \neq Hreceived$ **then return** $(false, st_P, \perp)$
- 5: set i to the smallest index such that $st_P^{rec,i} \neq \perp$
- 6: **if** $i + n > v$ **then return** $(false, st_P, \perp)$
- 7: **onion.Receive** $(hk, st_P^{rec,i}, \dots, st_P^{rec,i+n-1}, Hreceived, ct) \rightarrow (acc, st_P^{rec,i+n-1}, pt)$
- 8: **if** $acc = false$ **then return** $(false, st_P, \perp)$
- 9: parse $pt = (st_P^{send,u+1}, k)$ ▷ a new send state is added in the list
- 10: $st_P^{send,i}, \dots, st_P^{send,i+n-2} \leftarrow \perp$ ▷ n entries of st_P^{rec} were erased
- 11: $st_P^{rec,i+n-1} \leftarrow st_P^{rec,i+n-1}$ ▷ update st_P^{rec} stage 2: update $st_P^{rec,i+n}$
- 12: $Hreceived' \leftarrow H.Eval(hk, ct)$
- 13: $st_P' \leftarrow (hk, (st_P^{send,1}, \dots, st_P^{send,u+1}), (st_P^{rec,1}, \dots, st_P^{rec,v}), Hsent, Hreceived')$
- 14: **return** (acc, st_P', k)

- onion.decrypt with receive states (onion encryption)
- authenticate received hash and the onion depth
- remove all but the last used receive states
- get st^{send} and add in list

Example

	Alice		messages	Bob		
	send states	receive states		send states	receive states	
send k_1^A	$st_{1,0}^{A,S}$	$st_{1,0}^{A,R}$	$\rightarrow [st_{2,0}^{B,S}, k_1^A]_{st_{1,0}} \rightarrow$	$st_{1,0}^{B,S}$	$st_{1,0}^{B,R}$	
send k_2^A	$st_{1,1}^{A,S}$	$st_{1,0}^{A,R}, st_{2,0}^{A,R}$	$\rightarrow [st_{3,0}^{B,S}, k_2^A]_{st_{1,1}} \rightarrow$			
	$st_{1,2}^{A,S}$	$st_{1,0}^{A,R}, st_{2,0}^{A,R}, st_{3,0}^{A,R}$	$\leftarrow [st_{2,0}^{A,S}, k_1^B]_{st_{1,0}} \leftarrow$	$st_{1,1}^{B,S}$	$st_{1,0}^{B,R}, st_{2,0}^{B,R}$	send k_1^B
receive k_1^B	$st_{1,2}^{A,S}, st_{2,0}^{A,S}$	$st_{1,1}^{A,R}, st_{2,0}^{A,R}, st_{3,0}^{A,R}$				
			$\leftarrow [st_{3,0}^{A,S}, k_2^B]_{st_{1,1}, st_{2,0}, st_{3,0}} \leftarrow$	$st_{1,1}^{B,S}, st_{2,0}^{B,S}$	$st_{1,1}^{B,R}, st_{2,0}^{B,R}$	receive k_1^A
				$st_{1,1}^{B,S}, st_{2,0}^{B,S}, st_{3,0}^{B,S}$	$st_{1,2}^{B,R}, st_{2,0}^{B,R}$	receive k_2^A
				$st_{3,1}^{B,S}$	$st_{1,2}^{B,R}, st_{2,0}^{B,R}, st_{3,0}^{B,R}$	send k_2^B
receive k_2^B	$st_{1,2}^{A,S}, st_{2,0}^{A,S}, st_{3,0}^{A,S}$	$st_{3,1}^{A,R}$	$\rightarrow [st_{4,0}^{B,S}, k_3^A]_{st_{1,2}, st_{2,0}, st_{3,0}} \rightarrow$			
send k_3^A	$st_{3,1}^{A,S}$	$st_{3,1}^{A,R}, st_{4,0}^{A,R}$				
				$st_{3,1}^{B,S}, st_{4,0}^{B,S}$	$st_{3,1}^{B,R}$	receive k_3^A

FORGE Security

For all ppt \mathcal{A} , $\Pr[\text{FORGE}^{\mathcal{A}} \rightarrow 1] = \text{negl}$

Game $\text{FORGE}^{\mathcal{A}}$

- 1: Setup $\xrightarrow{\$}$ pp
- 2: Initall(pp) $\xrightarrow{\$}$ (st_A, st_B, z)
- 3: $(P, ct) \leftarrow \mathcal{A}^{\text{RATCH, EXP}_{st}, \text{EXP}_{key}}(z)$
- 4: **if** there is a participant NOT in a matching status **then return 0**
- 5: $\text{RATCH}(P, \text{rec}, ct) \rightarrow \text{acc}$
- 6: **if** acc = false **then return 0**
- 7: **if** P is in a matching status **then return 0**
- 8: **if** ct is a trivial forgery for P **then return 0**
- 9: **return 1**

This notion is interesting to have in order to reduce exclusion of forgeries to exclusion of trivial forgeries in KIND security:

$$(C_{\text{leak}} \wedge C_{\text{forge}}^*)\text{-KIND security} \stackrel{(+\text{FORGE})}{\implies} (C_{\text{leak}} \wedge C_{\text{trivial forge}}^*)\text{-KIND security}$$

RECOVER Security

For all ppt \mathcal{A} , $\Pr[\text{RECOVER}^{\mathcal{A}} \rightarrow 1] = \text{negl}$

Game $\text{RECOVER}^{\mathcal{A}}$

- 1: **Setup** $\xrightarrow{\$}$ pp
- 2: **Initall**(pp) $\xrightarrow{\$}$ $(\text{st}_A, \text{st}_B, z)$
- 3: **set all lists** to \emptyset
- 4: $P \leftarrow \mathcal{A}^{\text{RATCH, EXP}_{\text{st}}, \text{EXP}_{\text{key}}}(z)$
- 5: **if we can parse** as follows **then return** 1

$$\begin{aligned} \text{sent}_{\text{msg}}^{\bar{P}} &= ([\text{seq}_2], \text{ct}, [\text{seq}_3]) \\ &\qquad \qquad \qquad \text{‡} \quad \parallel \\ \text{received}_{\text{msg}}^P &= ([\text{seq}_1], \text{ct}) \end{aligned}$$

6: **return** 0

This notion is interesting to have in order to make sure that a round trip communication between honest participants implies no forgery.

$$(C_{\text{leak}} \wedge C_{\text{trivial forge}}^{A,B})\text{-KIND security} \stackrel{(+\text{RECOVER})}{\implies} (C_{\text{leak}} \wedge C_{\text{ratchet}})\text{-KIND security}$$

Security of BARK

Theorem

If

- H is collision-resistant,
- Sign is EF-OTCPA-secure,
- PKC is IND-CCA-secure,
- Sym is IND-OTCCA-secure,

then BARK is

- RECOVER-secure,
- FORGE-secure, and
- KIND-secure for cleanness $C_{\text{leak}} \wedge C_{\text{trivial forge}}^{A,B}$.



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ARCAD

Asynchronous Ratcheted Communication with Additional Data

- new interface for Send:

$$\text{Send}(st, ad, pt) \rightarrow st', ct$$

encrypt pt and authenticate ad at the same time

- new interface for Receive:

$$\text{Receive}(st, ad, ct) \rightarrow acc, st', pt$$

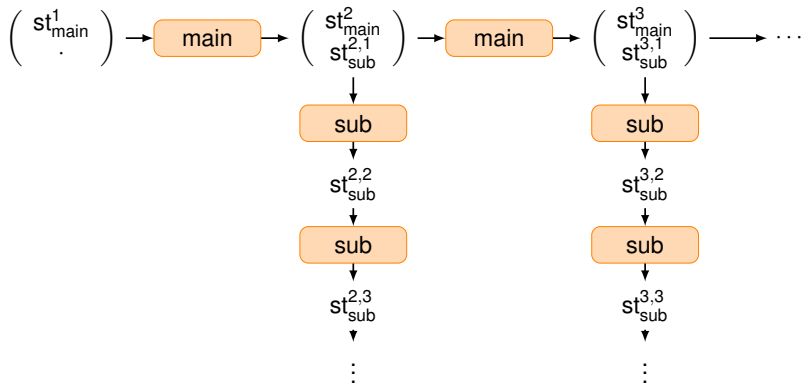
liteARCAD: Our Symmetric Protocol

- same as previous protocol with AE instead of SC
- much faster
- no post-compromise security
- still forward security

On-Demand Ratcheting

- use a flag in ad denoted by ad.flag
 - ad.flag = true: ratchet
 - ad.flag = false: live with symmetric crypto
- hybrid security notion...
 - adapt BARK as ARCAD_{DV} for ratchet
 - use liteARCAD for symmetric crypto

Hybrid Ratcheting



Hybrid Ratcheting: Results

- combining ARCAD_{DV} + liteARCAD, we obtain the best performances if we scarcely ratchet
- privacy is preserved (with hybrid cleanness...)
- unforgeability degrades a bit
- a final protocol transformation restores unforgeability

Security Awareness

- **r-RECOVER security**: cannot *receive* any genuine message after receiving a forgery
- **s-RECOVER security**: cannot *send* any genuine message after receiving a forgery
- **acknowledgement extractor**: each message carries an ACK of received messages
- **cleanness extractor**: can figure out which message remains private from the history of queries

→ achieved with hybrid ARCAD_{DV} + liteARCAD

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Implementations

ARCAD_{DV} uses ECDSA and ECIES.

liteARCAD uses AES-GCM.

PR18 uses Gentry-Silverberg HIBE and ECDSA.

JS18 uses Gentry-Silverberg HIBE and Bellare-Miner forward-secure signature.

ACD19 uses ECDH and AES-GCM

JMM19 uses ECDSA and ECIES

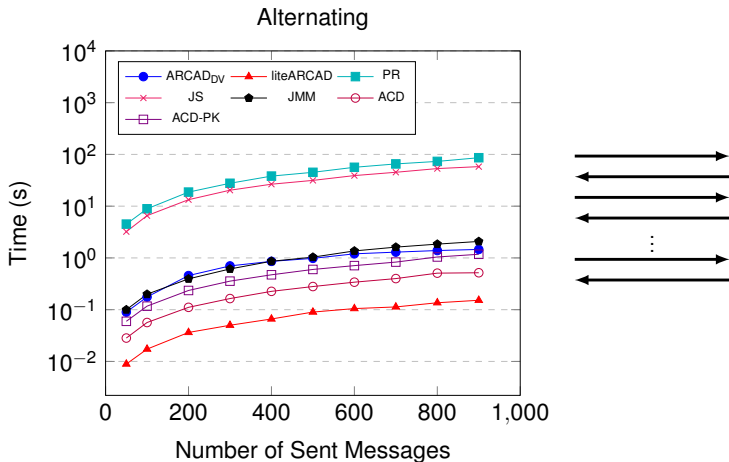
Acknowledgement: implementations by Andrea Caforio

<https://github.com/qantik/ratcheted>

Performance

Runtime

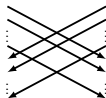
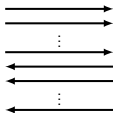
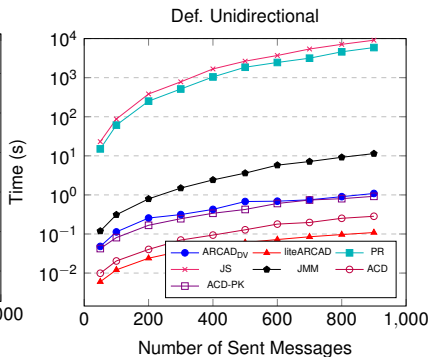
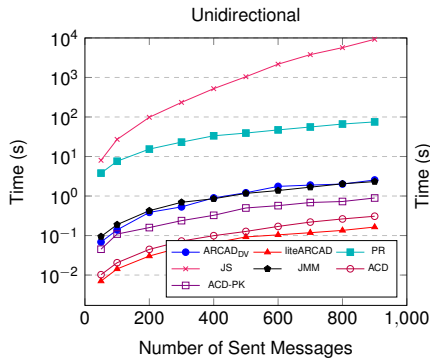
Total amount of time (log scale) to send n messages in alternating directions



Performance

Runtime

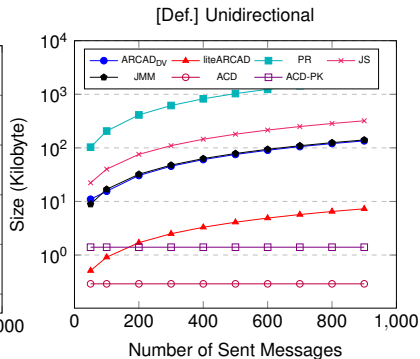
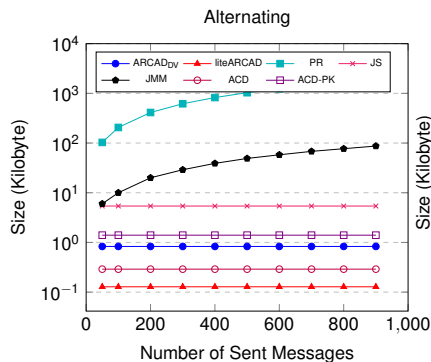
Total amount of time (log scale) to send n messages



Performance


State Size

Maximal state size (log scale) to send n messages



Comparison

ARCAD_{DV} + liteARCAD



	PR18	JS18	BARK	JMM19	ACD19-PK	ARCAD
Security	optimal	optimal	sub-optimal	near-optimal	id-optimal	pragmatic
Complexity	$\mathcal{O}(n^2)$	$\mathcal{O}(n^2)$	$\mathcal{O}(n)$	$\mathcal{O}(n^2)$	$\mathcal{O}(n)$	$\mathcal{O}(n)$
Corrupt coins resilience	no	pre-send ⇒ exposure	no	post-send	chosen coins ⇒ exposure	no
Plain model	no	no	yes	no	yes	yes
PKC or less	no	no	yes	yes	yes	yes
Immediate decryption	no	no	no	no	yes	no
r-RECOVER security	no	yes	yes	no	no	yes
s-RECOVER security	no	yes	no	no	no	yes
ack. extractor	yes	yes	yes	yes	no	yes
cleanness extractor	yes	yes	yes	yes	yes	yes

- Security: optimal > near-optimal > sub-optimal > pragmatic > id-optimal
- Complexity to send n messages in total
- Plain model: some need random oracles
- PKC or less: some need HIBE

Conclusion



- better understanding on ratcheting security
- ratcheting security can be efficient
- new notions: on-demand ratcheting, security awareness